

$$\mathcal{L}(\phi) \stackrel{=}{=} \mathcal{L}(C\phi) \stackrel{=}{=} \mathcal{L}(\rho(g)C\phi)$$