

$$Out(\mathbb{Z}_n) = \frac{Aut(\mathbb{Z}_n)}{Inn(\mathbb{Z}_n)} \equiv (\mathbb{Z}/n\mathbb{Z})^\times$$