

$$f(r^n) = f(r)^n = e \Rightarrow f_a(r) = r^a \mid \gcd(a, n) = 1$$